Unit 6 Group Work 2 PCHA 2022-23 / Dr. Kessner

No Calculator

- 1. Evaluate:
 - a. $\binom{7}{1}$
 - b. $\binom{7}{2}$
 - c. $\binom{7}{3}$
 - d. $\binom{7}{4}$
 - e. $\binom{12}{2}$
 - f. $\binom{12}{3}$
 - g. $\binom{12}{9}$
 - h. $\binom{12}{10}$
 - i. $\binom{100}{99}$
 - j. $\binom{2000}{2}$

- **2.** Let $\{a_k\}_{k=1}^{\infty} = \{\frac{1}{2}, -\frac{1}{4}, \frac{1}{8}, -\frac{1}{16}, \cdots\}.$
 - a. What type of sequence is this? Write recursive and explicit formulas for a_k .

b. Let S_n be the n^{th} partial sum of the sequence $\{a_k\}$. Express S_n (for this particular sequence) in summation notation.

c. Write a formula for the actual sum S_n (for this particular sequence).

d. What is the sum of the infinite series $\frac{1}{2} - \frac{1}{4} + \frac{1}{8} - \frac{1}{16} + \cdots$? (Surprising?)

3. Expand $(2 - x^2)^4$.

Find the x^6 term in $(2-x^2)^5$.

Find the x^8 term in $(2-x^2)^5$.

4. Suppose you have 7 red and 3 white marbles in a bag. You pick 6 of the marbles from the bag (without replacement).
a. What is the probability that you pick 6 red marbles?
b. What is the probability that you pick 4 red (and 2 white marbles)?
c. What is the probability that you pick 2 red marbles?

- 5. Suppose you have 9 black and 3 white marbles in a bag.
- **a.** You sample 5 marbles with replacement (in other words, you pick a marble, look at it, and put it back, 5 times). Let B be the number of times you pick a black marble. Calculate all of the 6 probabilities P(B=0), P(B=1), ..., P(B=5). Verify that $1 = \sum_{k=0}^{5} P(B=k)$.

b. This time you sample 5 marbles without replacement (in other words, you grab 5 marbles from the bag, all at the same time). Calculate the probabilities P(B=0), P(B=1), ..., P(B=5) and again verify that $1 = \sum_{k=0}^{5} P(B=k)$.