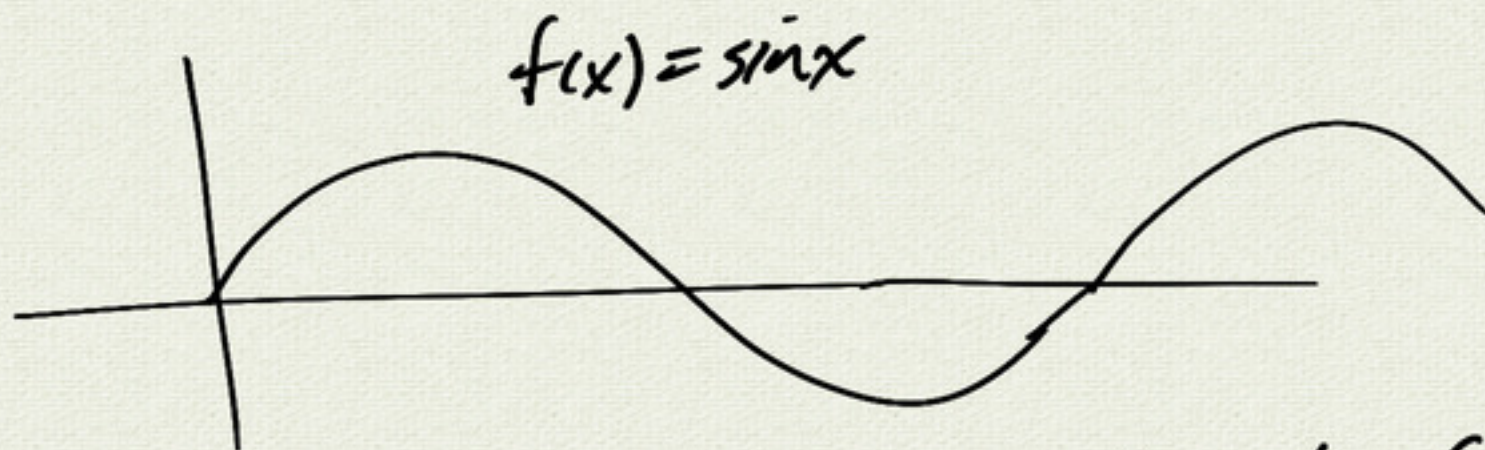


# 4.1 Function Properties

domain/range

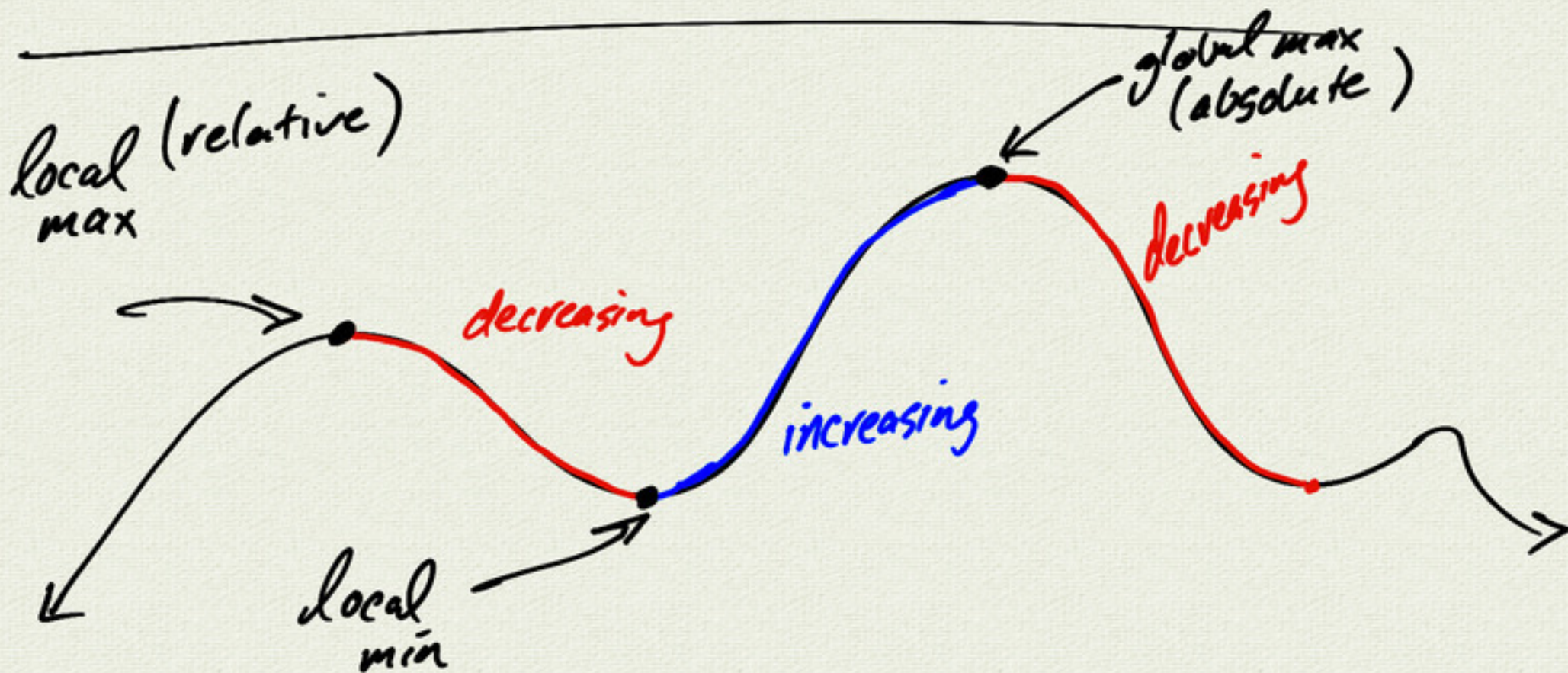


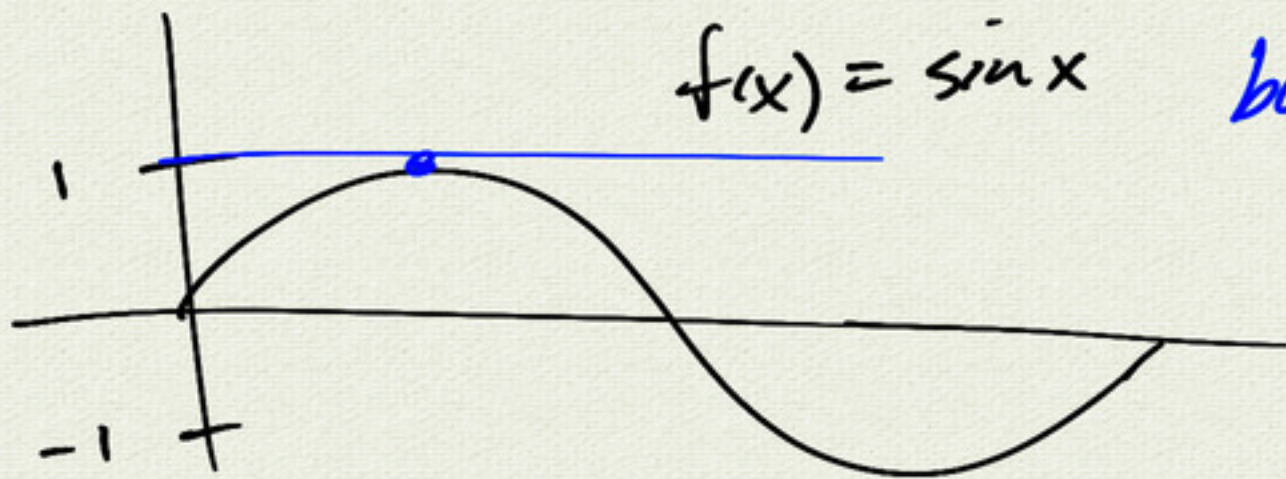
domain:  $\mathbb{R}$

range:  $[-1, 1]$

domain = where the function is defined

range = set of all possible function values



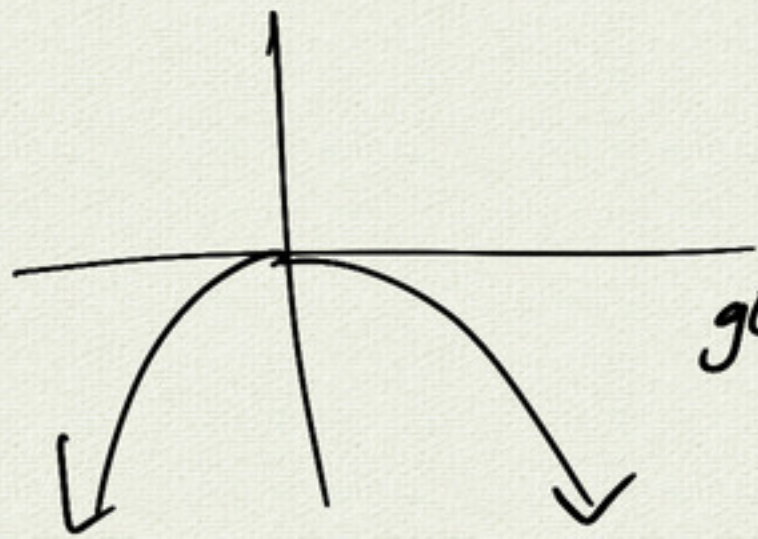


$$f(x) = \sin x$$

bounded above

bounded below

bounded: both above and below

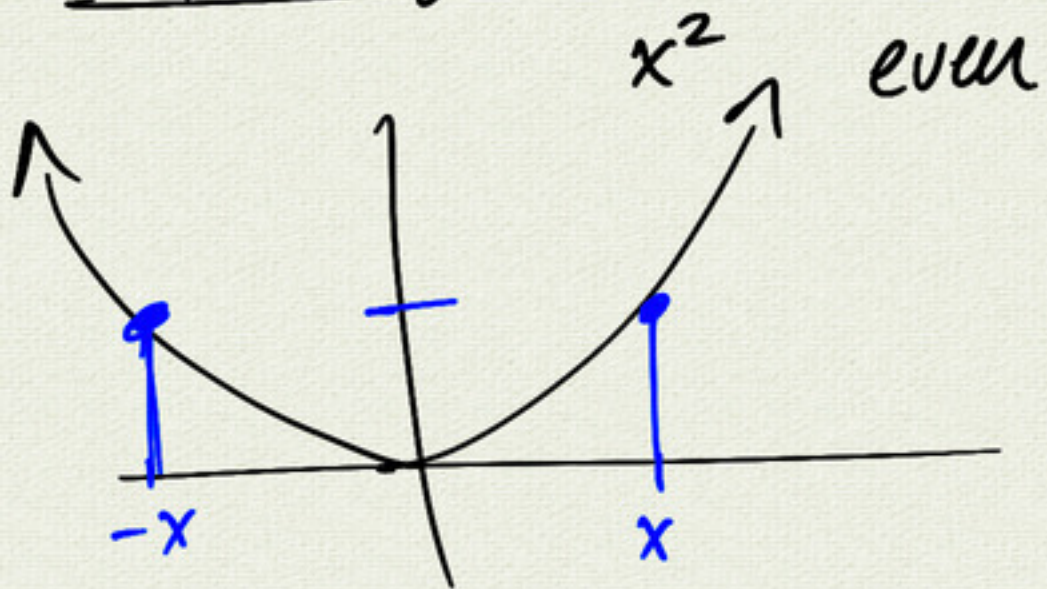


$$g(x) = -x^2$$

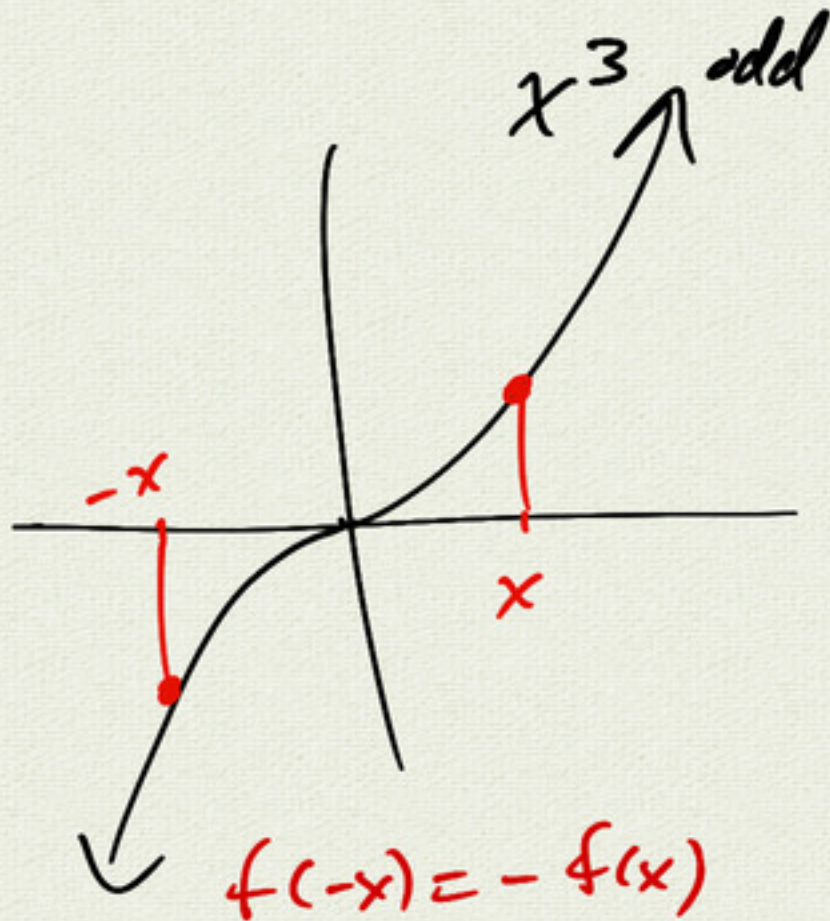
bounded above,  
but not below

(no lower bound)

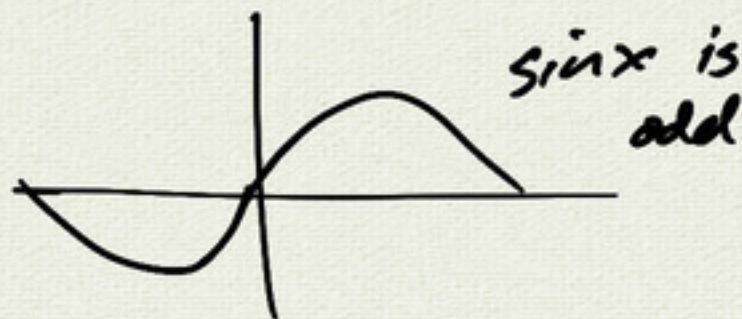
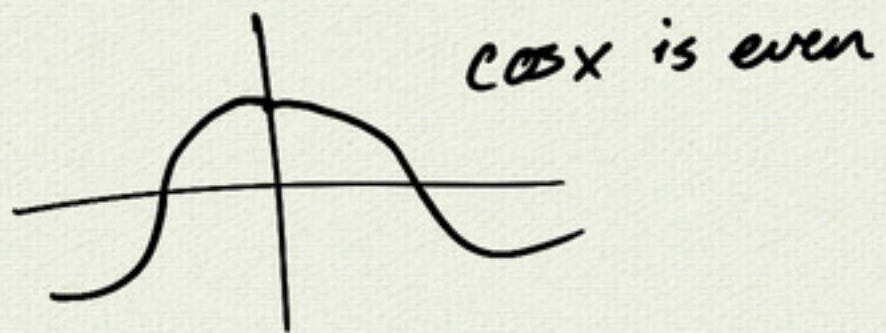
# odd/even symmetry



$$f(-x) = f(x)$$



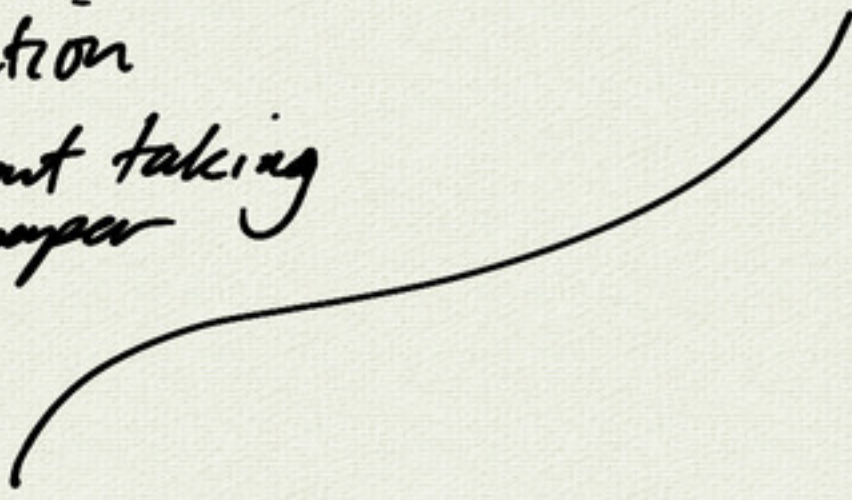
$$f(-x) = -f(x)$$



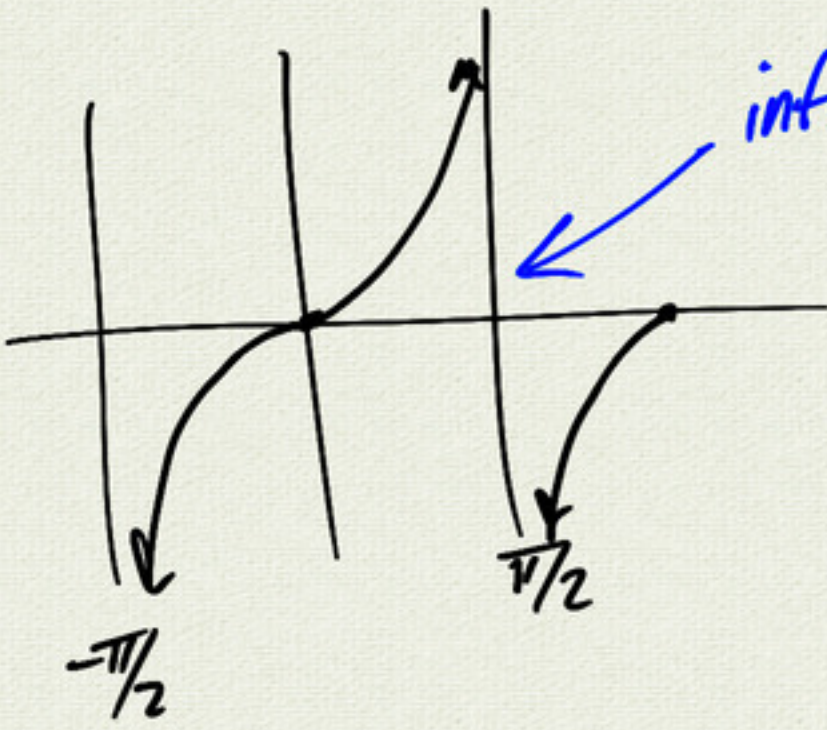
# discontinuities

continuous function

- draw without taking pen off paper

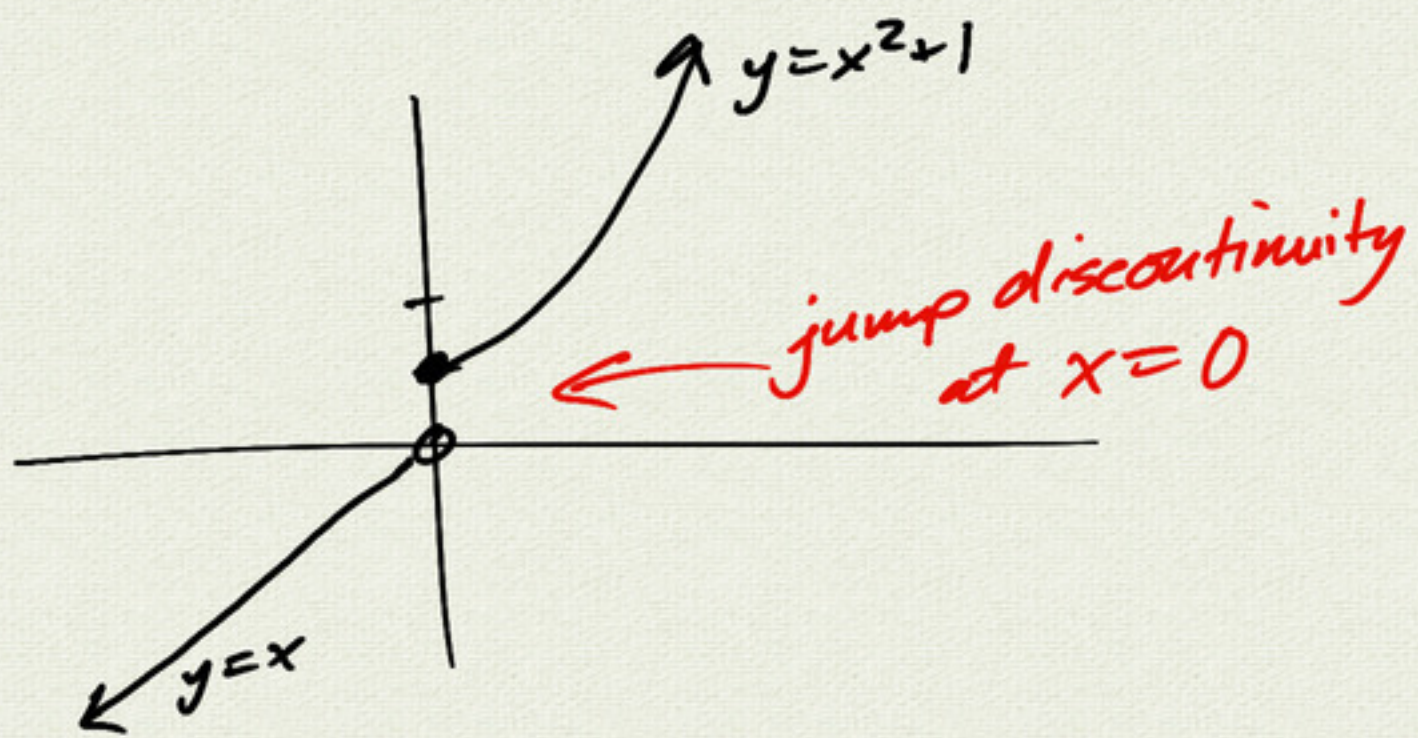


$\tan x$ :

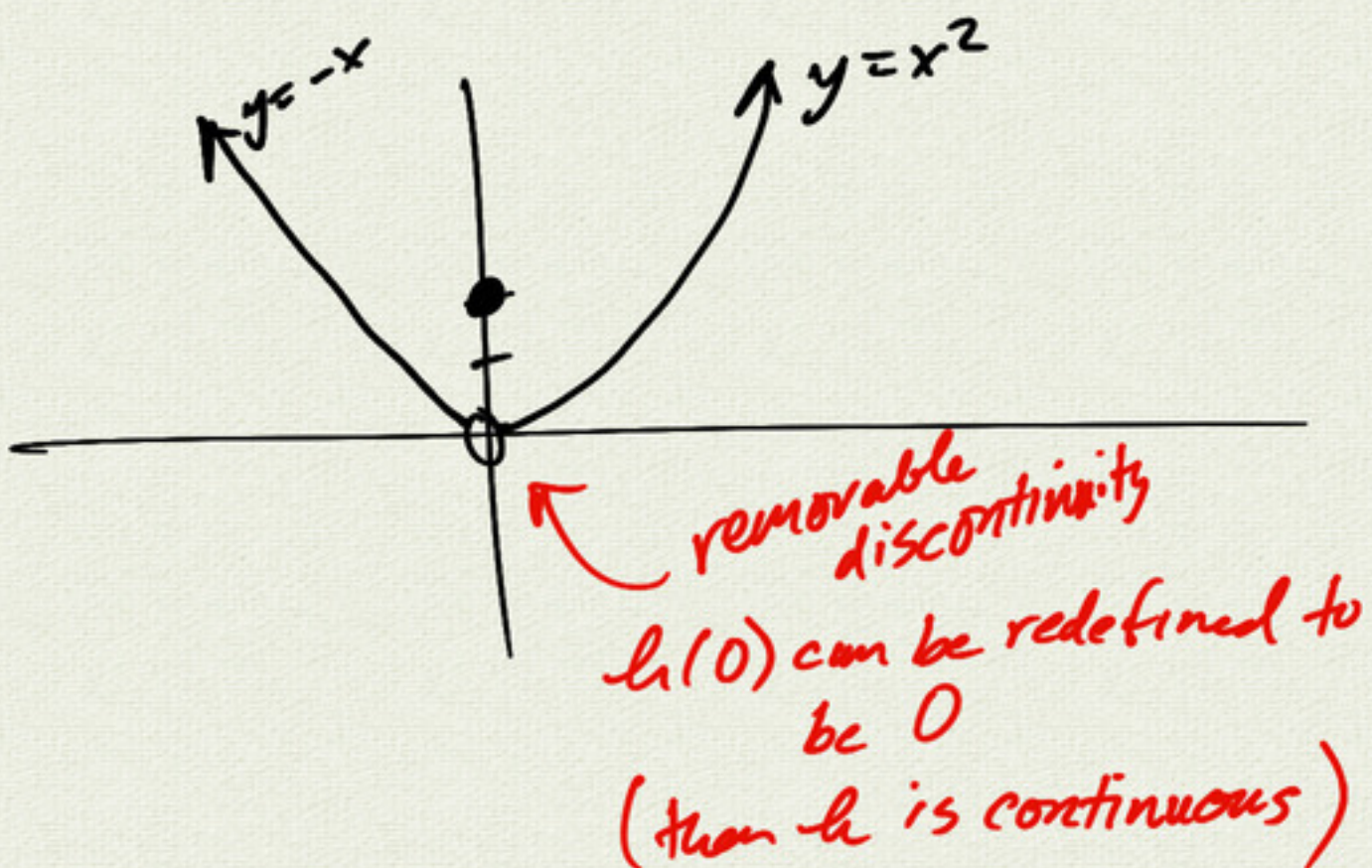


infinite discontinuity at  $x = \pi/2 + k\pi$  ( $k \in \mathbb{Z}$ )

let  $g(x) = \begin{cases} x & x < 0 \\ x^2 + 1 & x \geq 0 \end{cases}$  piecewise function



let  $h(x) = \begin{cases} -x & x < 0 \\ x^2 & x > 0 \\ 2 & x = 0 \end{cases}$



$\text{int}(x)$

greatest integer function  
(the biggest integer  $\leq x$ )

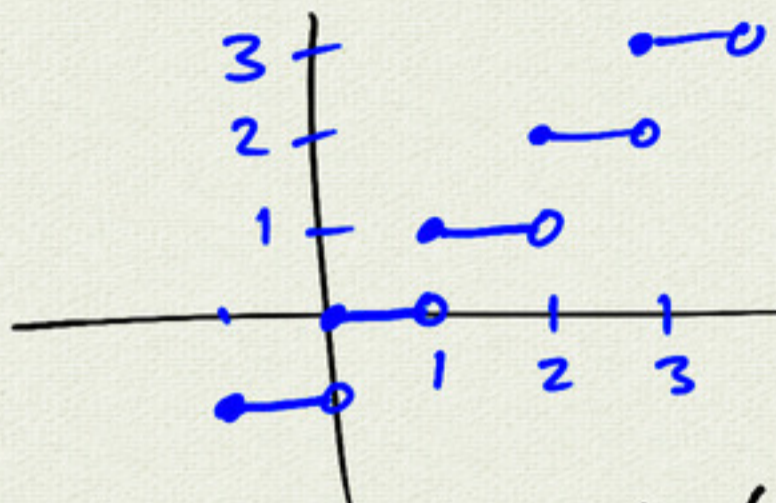
$$\text{int}(0) = 0$$

$$\text{int}(.1) = 0$$

$$\text{int}(.5) = 0$$

$$\text{int}(.9) = 0$$

$$\text{int}(1) = 1$$



step function

jump discontinuity at  $x = k$  ( $k \in \mathbb{Z}$ )

domain =  $\mathbb{R}$

range =  $\mathbb{Z}$

$$f(x) = \frac{1}{x}$$

$x$	$\frac{1}{x}$
1	1
10	.1
100	.01
1000	.001
<hr/>	
.1	10
.01	100
.001	1000

$$\lim_{x \rightarrow -\infty} f(x) = 0$$

$$\lim_{x \rightarrow 0^+} f(x) = \infty$$

$$\lim_{x \rightarrow 0^+} \frac{1}{x} = \infty$$

end behavior  
( $x \rightarrow \pm \infty$ )

$$\lim_{x \rightarrow \infty} \frac{1}{x} = 0$$

$$\lim_{x \rightarrow 0^-} f(x) = -\infty$$