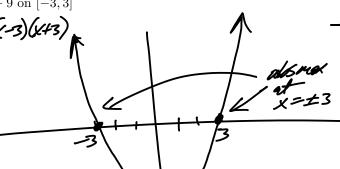
Unit 10 Group Work PCHA 2021-22 / Dr. Kessner

KEY

No calculator! Have fun!

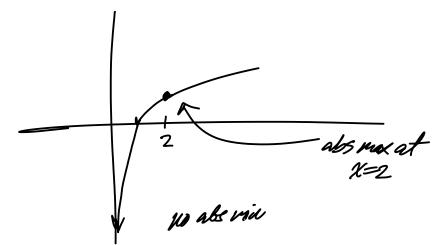
1. Graph the given function on the specified interval. Find all critical points. Identify any points where there is a local \min/\max , and verify with a derivative test. Identify the absolute \max and \min . If either fails to exist, state the condition of the Extreme Value Theorem that is not satisfied.

a. $g(x) = x^2 - 9$ on [-3, 3]



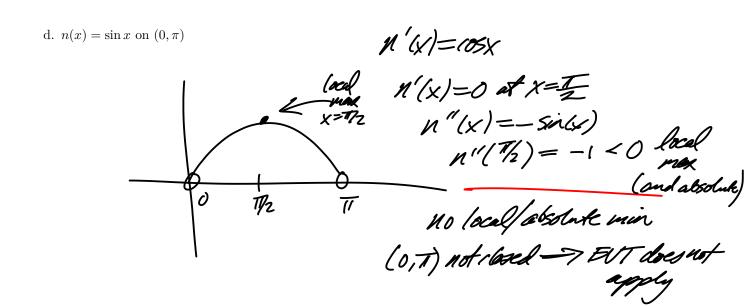
oritical pts: g'(x)=2x g'(x)=0=x=0 g''(x)=2 - g''(0)>0=2

b. $h(x) = \ln x$ on (0, 2]



 $\frac{L(x)=\frac{1}{x}}{27} \text{ no critical pts}$ on $\{0,2\}$

(0,2] not closed — EVT does not copply $m'(x) = \tan x \text{ on } [0, \pi]$ m'(x) = gcx $m'(x) = 0 \text{ at } x = 0, \pi$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \end{cases}$ $\text{Critical of } \begin{cases} \text{Critical of } \\ \text{Critical of } \end{cases}$ $\text{Critical of } \end{cases}$ $\text{Cr$



2. For each of the given functions find all antiderivatives.

a.
$$p'(x) = x^4$$

b.
$$q'(x) = \cos 2x$$

$$g(x) = \pm \sin 2x + C$$

c.
$$r'(x) = \frac{1}{x}$$

d.
$$s'(x) = \frac{1}{x^2}$$

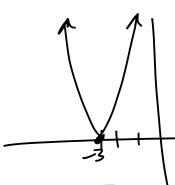
$$s(x) = -\frac{1}{x} + C$$

e.
$$t'(x) = e^{\frac{x}{3}}$$

$$f(x) = 3e^{x/3} + C$$

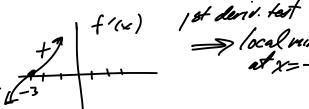
3. For each of the following functions: sketch the graph, then find all local extrema and verify with a derivative test.

a.
$$f(x) = (x+3)^4$$
.



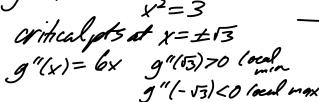
 $f'(x) = 4(x+3)^3$ f'(x) = 0 at x = -3 $f''(x) = 12(x+3)^2$ f''(0) = 0 inconclusive

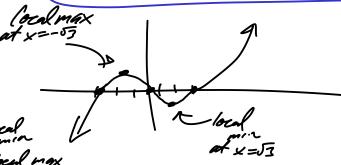
b.
$$g(x) = x^3 - 9x$$
. = $\times (x^2 - 9)$



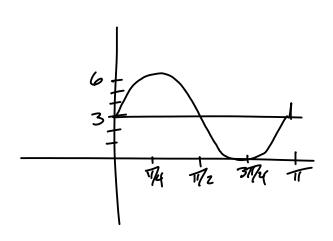
$$g'(x)=3x^{2}-9$$

 $g'(x)=0=3x^{2}=9$
 $x^{2}=3$



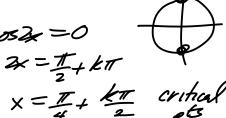


c. $h(x) = 3 + 3\sin 2x$. You may restrict your attention to the first period of the function. But as an extra challenge, identify *all* local extrema (not just the first period), including derivative tests to show which are minima and which are maxima.



$$f'(x) = 6\cos 2x$$

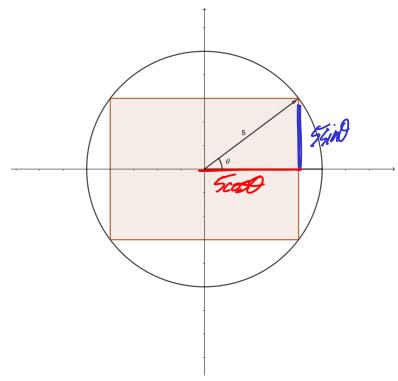
 $f'(x) = 0 \implies \cos 2x = 0$



$$A''(\frac{T}{4} + k\pi) = -12 \sin \frac{T}{2} = -2 < 0 \text{ local}$$

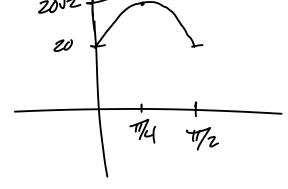
$$A''(\frac{3\pi}{4} + k\pi) = -12 \sin \frac{3\pi}{2} = 12 > 0 \text{ local}$$
win

4. Consider the following rectangle inscribed in a circle of radius 5. Note that the perimeter of the rectangle changes as the angle θ changes.



a. Write an equation for the perimeter $P(\theta)$ of the rectangle as a function of θ . Challenge: draw a sketch of the graph of $P(\theta)$ on $[0, \frac{\pi}{2}]$ by hand, and then check with graphing software.

P(0)= 4.551n0+ 4.51080 = 205m0+201080



b. Find the absolute min and max of the perimeter, for θ in $\left[0,\frac{\pi}{2}\right]$. Why must there be an absolute minimum and maximum?

P'(0)=20cost -20sin0

P(o) continuous

EVT

ou finite closed

interval [0,72]) abs madmin
exist in