

Unit 3 Group Work
PCHA 2021-22 / Dr. Kessner

Name / Pledge:

Partner(s):

You can use your notes and/or textbook. No calculator. Have fun!

1. Suppose you have the following vectors:

$$\vec{u} = \langle 2, 2\sqrt{3} \rangle$$

$$\vec{v} = \langle 3\sqrt{3}, -3 \rangle$$

$$\vec{w} = \langle 3, 0 \rangle$$

Calculate the following:

a) $|\vec{u}|$

b) $|\vec{v}|$

c) Unit vector in the direction of \vec{v} .

d) Angle between \vec{u} and \vec{v} .

e) Angle between \vec{u} and \vec{w} .

2. a) Parametrize the line segment from $(1, 2)$ to $(3, 6)$.

b) Parametrize the line segment from $(3, 6)$ to $(1, 2)$ (same points, opposite direction).

c) Parametrize the circle with center $(3, 4)$ and radius 5.

d) Parametrize the same circle, but make the period = 6.

3. Find all polar coordinates of the following (rectangular) points:

a) $(1, 1)$

b) $(-3\sqrt{3}, 3)$

Convert the following equations from rectangular to polar coordinates:

c) $3x + 4y = 5$

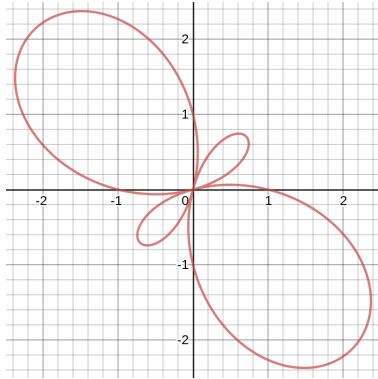
d) $x^2 + y^2 = 25$

Convert from polar to rectangular:

e) $r = -5 \sin \theta$

f) $r = 5 \csc \theta$

4. Analyze the graph of the polar function $r = 1 - 2 \sin 2\theta$:
- 1) Find the max $|r|$ values and θ values where they occur.
 - 2) State and prove any symmetry relations.
 - 3) **Challenge:** What is going on at $\frac{\pi}{4}$ and $\frac{5\pi}{4}$?



5. For each of the following 2x2 matrices, determine whether it is invertible, and if so, find the inverse matrix and the determinant of the inverse.

$$A = \begin{pmatrix} 3 & 0 \\ 0 & 3 \end{pmatrix}$$

$$B = \begin{pmatrix} -2 & 0 \\ 0 & 2 \end{pmatrix}$$

$$C = \begin{pmatrix} 0 & 2 \\ 2 & 0 \end{pmatrix}$$

$$D = \begin{pmatrix} 1 & 2 \\ 2 & 4 \end{pmatrix}$$

Let $E = \begin{pmatrix} 6 & 5 \\ 5 & 4 \end{pmatrix}$. Find E^{-1} . Verify that $EE^{-1} = I$.

Use the inverse matrix you found to solve the following linear systems:

$$\begin{aligned} 6x + 5y &= 1 \\ 5x + 4y &= 0 \end{aligned}$$

$$\begin{aligned} 6x + 5y &= 0 \\ 5x + 4y &= 1 \end{aligned}$$

$$\begin{aligned} 6x + 5y &= 1 \\ 5x + 4y &= 2 \end{aligned}$$

6. Consider the following system of linear equations:

$$\begin{aligned}x + 3z &= 4 \\-x - 2z &= -3 \\y - 2z &= -1\end{aligned}$$

a. Write the linear system as a matrix equation.

b. Calculate the determinant of the matrix to verify that the matrix is invertible.

c. Find the inverse matrix and use it to solve the system.